

Øgsl'sf *- texinfo *-

`gsl_sf ()` [Loadable Function]

Octave bindings to the GNU Scientific Library. All GSL functions can be called with by the GSL names within octave.

Øclausen *- texinfo *-

`y = clausen (x)` [Loadable Function]

`[y, err] = clausen (...)` [Loadable Function]

The Clausen function is defined by the following integral,

$$\text{Cl}'_2(x) = - \int_0^x dt \log(2 \sin(t/2))$$

It is related to the dilogarithm by $\text{Cl}'_2(\theta) = \text{Im Li}'_2(\exp(i \theta))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødawson *- texinfo *-

`y = dawson (x)` [Loadable Function]

`[y, err] = dawson (...)` [Loadable Function]

The Dawson integral is defined by $\exp(-x^2) \int_0^x dt \exp(t^2)$. A table of Dawson integral can be found in Abramowitz & Stegun, Table 7.5.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'1 *- texinfo *-

`y = debye_1 (x)` [Loadable Function]

`[y, err] = debye_1 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D'_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'2 *- texinfo *-

`y = debye_2 (x)` [Loadable Function]

`[y, err] = debye_2 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D'_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'3 *- texinfo *-

`y = debye_3 (x)` [Loadable Function]
`[y, err] = debye_3 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'4 *- texinfo *-

`y = debye_4 (x)` [Loadable Function]
`[y, err] = debye_4 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf'gsl *- texinfo *-

`y = erf_gsl (x)` [Loadable Function]
`[y, err] = erf_gsl (...)` [Loadable Function]

These routines compute the error function $\text{erf}(x) = (2/\sqrt{\pi}) \int_0^x dt \exp(-t^2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerfc'gsl *- texinfo *-

`y = erfc_gsl (x)` [Loadable Function]
`[y, err] = erfc_gsl (...)` [Loadable Function]

These routines compute the complementary error function $\text{erfc}(x) = 1 - \text{erf}(x) = (2/\sqrt{\pi}) \int_x^\infty \exp(-t^2) dt$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog'erfc *- texinfo *-

`y = log_erfc (x)` [Loadable Function]
`[y, err] = log_erfc (...)` [Loadable Function]

These routines compute the logarithm of the complementary error function $\log(\text{erfc}(x))$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf_Z *- texinfo *-

y = erf_Z (*x*) [Loadable Function]
[*y*, *err*] = erf_Z (...) [Loadable Function]

These routines compute the Gaussian probability function $Z(x) = (1/(2\pi)) \exp(-x^2/2)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf_Q *- texinfo *-

y = erf_Q (*x*) [Loadable Function]
[*y*, *err*] = erf_Q (...) [Loadable Function]

These routines compute the upper tail of the Gaussian probability function $Q(x) = (1/(2\pi)) \int x^{\infty} dt \exp(-t^2/2)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhazard *- texinfo *-

y = hazard (*x*) [Loadable Function]
[*y*, *err*] = hazard (...) [Loadable Function]

The hazard function for the normal distribution, also known as the inverse Mill's ratio, is defined as $h(x) = Z(x)/Q(x) = \sqrt{2/\pi} \exp(-x^2/2) / \operatorname{erfc}(x/\sqrt{2})$. It decreases rapidly as *x* approaches $-\infty$ and asymptotes to *h*(*x*) $\sim x$ as *x* approaches $+\infty$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpm1 *- texinfo *-

y = expm1 (*x*) [Loadable Function]
[*y*, *err*] = expm1 (...) [Loadable Function]

These routines compute the quantity $\exp(x)-1$ using an algorithm that is accurate for small *x*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel *- texinfo *-

`y = exprel (x)` [Loadable Function]

`[y, err] = exprel (...)` [Loadable Function]

These routines compute the quantity $(\exp(x)-1)/x$ using an algorithm that is accurate for small x . For small x the algorithm is based on the expansion $(\exp(x)-1)/x = 1 + x/2 + x^2/(2*3) + x^3/(2*3*4) + \dots$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel`2 -*- texinfo -*-

`y = exprel_2 (x)` [Loadable Function]

`[y, err] = exprel_2 (...)` [Loadable Function]

These routines compute the quantity $2(\exp(x)-1-x)/x^2$ using an algorithm that is accurate for small x . For small x the algorithm is based on the expansion $2(\exp(x)-1-x)/x^2 = 1 + x/3 + x^2/(3*4) + x^3/(3*4*5) + \dots$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`E1 -*- texinfo -*-

`y = expint_E1 (x)` [Loadable Function]

`[y, err] = expint_E1 (...)` [Loadable Function]

These routines compute the exponential integral $E_1(x)$,

$E_1(x) := \operatorname{Re} \int_1^{\infty} dt \exp(-xt)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`E2 -*- texinfo -*-

`y = expint_E2 (x)` [Loadable Function]

`[y, err] = expint_E2 (...)` [Loadable Function]

These routines compute the second-order exponential integral $E_2(x)$,

$E_2(x) := \operatorname{Re} \int_1^{\infty} dt \exp(-xt)/t^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`Ei -*- texinfo -*-

`y = expint_Ei (x)` [Loadable Function]

`[y, err] = expint_Ei (...)` [Loadable Function]

These routines compute the exponential integral $E_i(x)$,

$E_i(x) := -\operatorname{PV}(\int_{-x}^{\infty} dt \exp(-t)/t)$

where PV denotes the principal value of the integral.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØShi *-*- texinfo -*-*

y = Shi (*x*) [Loadable Function]

[*y*, *err*] = Shi (...) [Loadable Function]

These routines compute the integral $\text{Shi}(x) = \int_0^x dt \sinh(t)/t$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØChi *-*- texinfo -*-*

y = Chi (*x*) [Loadable Function]

[*y*, *err*] = Chi (...) [Loadable Function]

These routines compute the integral

$\text{Chi}(x) := \text{Re}[\gamma'E + \log(x) + \int_0^x dt (\cosh[t]-1)/t]$,

where $\gamma'E$ is the Euler constant.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'3 *-*- texinfo -*-*

y = expint_3 (*x*) [Loadable Function]

[*y*, *err*] = expint_3 (...) [Loadable Function]

These routines compute the exponential integral $\text{Ei}'_3(x) = \int_0^x dt \exp(-t^3)$ for $x \geq 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØSi *-*- texinfo -*-*

y = Si (*x*) [Loadable Function]

[*y*, *err*] = Si (...) [Loadable Function]

These routines compute the Sine integral $\text{Si}(x) = \int_0^x dt \sin(t)/t$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØCi *-*- texinfo -*-*

`y = Ci (x)` [Loadable Function]

`[y, err] = Ci (...)` [Loadable Function]

These routines compute the Cosine integral $Ci(x) = -\int_x^\infty dt \cos(t)/t$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øatanint -*- texinfo -*-

`y = atanint (x)` [Loadable Function]

`[y, err] = atanint (...)` [Loadable Function]

These routines compute the Arctangent integral $AtanInt(x) = \int_0^x dt \arctan(t)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi_dirac_mhalf -*- texinfo -*-

`y = fermi_dirac_mhalf (x)` [Loadable Function]

`[y, err] = fermi_dirac_mhalf (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{-1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi_dirac_half -*- texinfo -*-

`y = fermi_dirac_half (x)` [Loadable Function]

`[y, err] = fermi_dirac_half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi_dirac_3half -*- texinfo -*-

`y = fermi_dirac_3half (x)` [Loadable Function]

`[y, err] = fermi_dirac_3half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{3/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma_gsl -*- texinfo -*-

`y = gamma_gsl (x)` [Loadable Function]

`[y, err] = gamma_gsl (...)` [Loadable Function]

These routines compute the Gamma function $\Gamma(x)$, subject to x not being a negative integer. The function is computed using the real Lanczos method. The maximum value of x such that $\Gamma(x)$ is not considered an overflow is given by the macro `GSL_SF_GAMMA_XMAX` and is 171.0.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølngamma`gsl`-*` texinfo`-*`

`y = lngamma_gsl (x)` [Loadable Function]

`[y, err] = lngamma_gsl (...)` [Loadable Function]

These routines compute the logarithm of the Gamma function, $\log(\Gamma(x))$, subject to x not being negative integer. For $x < 0$ the real part of $\log(\Gamma(x))$ is returned, which is equivalent to $\log(|\Gamma(x)|)$. The function is computed using the real Lanczos method.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgammastar`-*` texinfo`-*`

`y = gammastar (x)` [Loadable Function]

`[y, err] = gammastar (...)` [Loadable Function]

These routines compute the regulated Gamma Function $\Gamma^*(x)$ for $x > 0$. The regulated gamma function is given by,

$$\Gamma^*(x) = \Gamma(x) / (\sqrt{2\pi} x^{\{x-1/2\}} \exp(-x)) = (1 + (1/12x) + \dots)$$
 for x to infity

and is a useful suggestion of Temme.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgammainv`gsl`-*` texinfo`-*`

`y = gammainv_gsl (x)` [Loadable Function]

`[y, err] = gammainv_gsl (...)` [Loadable Function]

These routines compute the reciprocal of the gamma function, $1/\Gamma(x)$ using the real Lanczos method.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølambert`W0`-*` texinfo`-*`

`y = lambert_W0 (x)` [Loadable Function]
`[y, err] = lambert_W0 (...)` [Loadable Function]

These compute the principal branch of the Lambert W function, $W^0(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x)\exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W^0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W^{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølambert`Wm1 -*- texinfo -*-

`y = lambert_Wm1 (x)` [Loadable Function]
`[y, err] = lambert_Wm1 (...)` [Loadable Function]

These compute the secondary real-valued branch of the Lambert W function, $W^{-1}(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x)\exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W^0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W^{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog`1plusx -*- texinfo -*-

`y = log_1plusx (x)` [Loadable Function]
`[y, err] = log_1plusx (...)` [Loadable Function]

These routines compute $\log(1 + x)$ for $x > -1$ using an algorithm that is accurate for small *x*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog`1plusx`mx -*- texinfo -*-

`y = log_1plusx_mx (x)` [Loadable Function]
`[y, err] = log_1plusx_mx (...)` [Loadable Function]

These routines compute $\log(1 + x) - x$ for $x > -1$ using an algorithm that is accurate for small *x*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi -*- texinfo -*-

`y = psi (x)` [Loadable Function]

`[y, err] = psi (...)` [Loadable Function]

These routines compute the digamma function $\psi(x)$ for general x , $x \in \mathbb{R}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi`1piy`*- texinfo`*-`

`y = psi_1piy (x)` [Loadable Function]

`[y, err] = psi_1piy (...)` [Loadable Function]

These routines compute the real part of the digamma function on the line $1+i y$, $\operatorname{Re}[\psi(1 + i y)]$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron`1`*- texinfo`*-`

`y = synchrotron_1 (x)` [Loadable Function]

`[y, err] = synchrotron_1 (...)` [Loadable Function]

These routines compute the first synchrotron function $x \int_0^x dt K_{5/3}(t)$ for $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron`2`*- texinfo`*-`

`y = synchrotron_2 (x)` [Loadable Function]

`[y, err] = synchrotron_2 (...)` [Loadable Function]

These routines compute the second synchrotron function $x K_{2/3}(x)$ for $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`2`*- texinfo`*-`

`y = transport_2 (x)` [Loadable Function]

`[y, err] = transport_2 (...)` [Loadable Function]

These routines compute the transport function $J(2,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^{-t} / (e^{-t} - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`3`*- texinfo`*-`

`y = transport_3 (x)` [Loadable Function]
`[y, err] = transport_3 (...)` [Loadable Function]

These routines compute the transport function $J(3,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`4`-*- texinfo`-`-

`y = transport_4 (x)` [Loadable Function]
`[y, err] = transport_4 (...)` [Loadable Function]

These routines compute the transport function $J(4,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`5`-*- texinfo`-`-

`y = transport_5 (x)` [Loadable Function]
`[y, err] = transport_5 (...)` [Loadable Function]

These routines compute the transport function $J(5,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsinc`gsl`-*- texinfo`-`-

`y = sinc_gsl (x)` [Loadable Function]
`[y, err] = sinc_gsl (...)` [Loadable Function]

These routines compute $\text{sinc}(x) = \sin(\pi x) / (\pi x)$ for any value of `x`.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnsinh`-`- texinfo`-`-

`y = lnsinh (x)` [Loadable Function]
`[y, err] = lnsinh (...)` [Loadable Function]

These routines compute $\log(\sinh(x))$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølncosh *-*- texinfo -*-*

`y = lncosh (x)` [Loadable Function]
`[y, err] = lncosh (...)` [Loadable Function]

These routines compute $\log(\cosh(x))$ for any x .

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta *-*- texinfo -*-*

`y = zeta (x)` [Loadable Function]
`[y, err] = zeta (...)` [Loadable Function]

These routines compute the Riemann zeta function $\zeta(s)$ for arbitrary s , $s > 1$.

The Riemann zeta function is defined by the infinite sum $\zeta(s) = \sum_{k=1}^{\infty} k^{-s}$.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta *-*- texinfo -*-*

`y = eta (x)` [Loadable Function]
`[y, err] = eta (...)` [Loadable Function]

These routines compute the eta function $\eta(s)$ for arbitrary s .

The eta function is defined by $\eta(s) = (1-2^{1-s}) \zeta(s)$.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Jn *-*- texinfo -*-*

`y = bessel_Jn (n, x)` [Loadable Function]
`[y, err] = bessel_Jn (...)` [Loadable Function]

These routines compute the regular cylindrical Bessel function of order n , $J_n(x)$.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Yn *-*- texinfo -*-*

`y = bessel_Yn (n, x)` [Loadable Function]
`[y, err] = bessel_Yn (...)` [Loadable Function]

These routines compute the irregular cylindrical Bessel function of order n , $Y_n(x)$, for $x > 0$.

err contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_In *- texinfo *-

`y = bessel_In (n, x)` [Loadable Function]

`[y, err] = bessel_In (...)` [Loadable Function]

These routines compute the regular modified cylindrical Bessel function of order n , $I_n(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_In_scaled *- texinfo *-

`y = bessel_In_scaled (n, x)` [Loadable Function]

`[y, err] = bessel_In_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified cylindrical Bessel function of order n , $\exp(-|x|) I_n(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Kn *- texinfo *-

`y = bessel_Kn (n, x)` [Loadable Function]

`[y, err] = bessel_Kn (...)` [Loadable Function]

These routines compute the irregular modified cylindrical Bessel function of order n , $K_n(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Kn_scaled *- texinfo *-

`y = bessel_Kn_scaled (n, x)` [Loadable Function]

`[y, err] = bessel_Kn_scaled (...)` [Loadable Function]

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_jl *- texinfo *-

`y = bessel_jl (n, x)` [Loadable Function]

`[y, err] = bessel_jl (...)` [Loadable Function]

These routines compute the regular spherical Bessel function of order l , $j_l(x)$, for $l \geq 0$ and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`yl`-* texinfo`-*`-

`y = bessel_yl (n, x)` [Loadable Function]

`[y, err] = bessel_yl (...)` [Loadable Function]

These routines compute the irregular spherical Bessel function of order l , $y_l(x)$, for $l \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`il`scaled`-* texinfo`-*`-

`y = bessel_il_scaled (n, x)` [Loadable Function]

`[y, err] = bessel_il_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified spherical Bessel function of order l , $\exp(-|x|) i_l(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`kl`scaled`-* texinfo`-*`-

`y = bessel_kl_scaled (n, x)` [Loadable Function]

`[y, err] = bessel_kl_scaled (...)` [Loadable Function]

These routines compute the scaled irregular modified spherical Bessel function of order l , $\exp(x) k_l(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel`n`-* texinfo`-*`-

`y = exprel_n (n, x)` [Loadable Function]

`[y, err] = exprel_n (...)` [Loadable Function]

These routines compute the N -relative exponential, which is the n -th generalization of the functions `gsl_sf_exprel` and `gsl_sf_exprel2`. The N -relative exponential is given by,

$$\text{exprel}^N(x) = N! / x^N (\exp(x) - \sum_{k=0}^{N-1} x^k / k!) = 1 + x / (N+1) + x^2 / ((N+1)(N+2)) + \dots = {}_1F_1(1, 1+N, x)$$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`int`-* texinfo`-*`-

`y = fermi_dirac_int (n, x)` [Loadable Function]
`[y, err] = fermi_dirac_int (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral with an integer index of j ,
 $F^j(x) = (1/\Gamma(j+1)) \int_0^\infty dt (t^j / (\exp(t-x)+1))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtaylorcoeff -*- texinfo -*-

`y = taylorcoeff (n, x)` [Loadable Function]
`[y, err] = taylorcoeff (...)` [Loadable Function]

These routines compute the Taylor coefficient $x^n / n!$ for $x \geq 0$, $n \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre_P1 -*- texinfo -*-

`y = legendre_P1 (n, x)` [Loadable Function]
`[y, err] = legendre_P1 (...)` [Loadable Function]

These functions evaluate the Legendre polynomial $P_l(x)$ for a specific value of l , x subject to $l \geq 0$, $|x| \leq 1$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre_Q1 -*- texinfo -*-

`y = legendre_Q1 (n, x)` [Loadable Function]
`[y, err] = legendre_Q1 (...)` [Loadable Function]

These routines compute the Legendre function $Q_l(x)$ for $x > -1$, $x \neq 1$ and $l \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi_n -*- texinfo -*-

`y = psi_n (n, x)` [Loadable Function]
`[y, err] = psi_n (...)` [Loadable Function]

These routines compute the polygamma function $\psi^{(m)}(x)$ for $m \geq 0$, $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Jnu -*- texinfo -*-

`z = bessel_Jnu (x, y)` [Loadable Function]
`[z, err] = bessel_Jnu (...)` [Loadable Function]

These routines compute the regular cylindrical Bessel function of fractional order ν , $J_\nu(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ø**bessel_Ynu** *- texinfo *-

`z = bessel_Ynu (x, y)` [Loadable Function]
`[z, err] = bessel_Ynu (...)` [Loadable Function]

These routines compute the irregular cylindrical Bessel function of fractional order ν , $Y_\nu(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ø**bessel_Inu** *- texinfo *-

`z = bessel_Inu (x, y)` [Loadable Function]
`[z, err] = bessel_Inu (...)` [Loadable Function]

These routines compute the regular modified Bessel function of fractional order ν , $I_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ø**bessel_Inu_scaled** *- texinfo *-

`z = bessel_Inu_scaled (x, y)` [Loadable Function]
`[z, err] = bessel_Inu_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified Bessel function of fractional order ν , $\exp(-|x|)I_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ø**bessel_Knu** *- texinfo *-

`z = bessel_Knu (x, y)` [Loadable Function]
`[z, err] = bessel_Knu (...)` [Loadable Function]

These routines compute the irregular modified Bessel function of fractional order ν , $K_\nu(x)$ for $x>0$, $u>0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`lnKnu`-*` texinfo`-*`

`z = bessel_lnKnu (x, y)` [Loadable Function]

`[z, err] = bessel_lnKnu (...)` [Loadable Function]

These routines compute the logarithm of the irregular modified Bessel function of fractional order ν , $\ln(K_\nu(x))$ for $x > 0$, $\nu > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Knu`scaled`-*` texinfo`-*`

`z = bessel_Knu_scaled (x, y)` [Loadable Function]

`[z, err] = bessel_Knu_scaled (...)` [Loadable Function]

These routines compute the scaled irregular modified Bessel function of fractional order ν , $\exp(+|x|) K_\nu(x)$ for $x > 0$, $\nu > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexp`mult`-*` texinfo`-*`

`z = exp_mult (x, y)` [Loadable Function]

`[z, err] = exp_mult (...)` [Loadable Function]

These routines exponentiate `x` and multiply by the factor `y` to return the product $y \exp(x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`inc`0`-*` texinfo`-*`

`z = fermi_dirac_inc_0 (x, y)` [Loadable Function]

`[z, err] = fermi_dirac_inc_0 (...)` [Loadable Function]

These routines compute the incomplete Fermi-Dirac integral with an index of zero, $F_0(x, b) = \ln(1 + e^{-b-x}) - (b-x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpoch`-*` texinfo`-*`

`z = poch (x, y)` [Loadable Function]

`[z, err] = poch (...)` [Loadable Function]

These routines compute the Pochhammer symbol

$(a)_x := \Gamma(a + x) / \Gamma(a)$,

subject to `a` and `a+x` not being negative integers. The Pochhammer symbol is also known as the Apell symbol.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnpoch *-*- texinfo -*-*

z = `lnpoch` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `lnpoch` (...) [Loadable Function]

These routines compute the logarithm of the Pochhammer symbol, $\log((a)_x) = \log(\Gamma(a+x)/\Gamma(a))$ for $a > 0$, $a+x > 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpochrel *-*- texinfo -*-*

z = `pochrel` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `pochrel` (...) [Loadable Function]

These routines compute the relative Pochhammer symbol $((a)_x - 1)/x$ where $(a)_x := \Gamma(a+x)/\Gamma(a)$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`Q *-*- texinfo -*-*

z = `gamma_inc_Q` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `gamma_inc_Q` (...) [Loadable Function]

These routines compute the normalized incomplete Gamma Function $Q(a,x) = 1/\Gamma(a) \int_0^x t^{a-1} \exp(-t) dt$ for $a > 0$, $x \geq 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`P *-*- texinfo -*-*

z = `gamma_inc_P` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `gamma_inc_P` (...) [Loadable Function]

These routines compute the complementary normalized incomplete Gamma Function $P(a,x) = 1/\Gamma(a) \int_0^x t^{a-1} \exp(-t) dt$ for $a > 0$, $x \geq 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc *-*- texinfo -*-*

`z = gamma_inc (x, y)` [Loadable Function]

`[z, err] = gamma_inc (...)` [Loadable Function]

These functions compute the incomplete Gamma Function the normalization factor included in the previously defined functions: $\Gamma(a, x) = \int_0^x t^{a-1} \exp(-t) dt$ for a real and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbeta`gsl`-*` texinfo`-*`

`z = beta_gsl (x, y)` [Loadable Function]

`[z, err] = beta_gsl (...)` [Loadable Function]

These routines compute the Beta Function, $B(a, b) = \Gamma(a)\Gamma(b)/\Gamma(a+b)$ for $a > 0$, $b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnbeta`-*` texinfo`-*`

`z = lnbeta (x, y)` [Loadable Function]

`[z, err] = lnbeta (...)` [Loadable Function]

These routines compute the logarithm of the Beta Function, $\log(B(a, b))$ for $a > 0$, $b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`0F1`-*` texinfo`-*`

`z = hyperg_0F1 (x, y)` [Loadable Function]

`[z, err] = hyperg_0F1 (...)` [Loadable Function]

These routines compute the hypergeometric function ${}_0F_1(c, x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP`half`-*` texinfo`-*`

`z = conicalP_half (x, y)` [Loadable Function]

`[z, err] = conicalP_half (...)` [Loadable Function]

These routines compute the irregular Spherical Conical Function $P^{-1/2}_{-1/2 + i\lambda}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP`mhalf -*- texinfo -*-

`z = conicalP_mhalf (x, y)` [Loadable Function]
`[z, err] = conicalP_mhalf (...)` [Loadable Function]

These routines compute the regular Spherical Conical Function $P^{-1/2}\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP`0 -*- texinfo -*-

`z = conicalP_0 (x, y)` [Loadable Function]
`[z, err] = conicalP_0 (...)` [Loadable Function]

These routines compute the conical function $P^0\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP`1 -*- texinfo -*-

`z = conicalP_1 (x, y)` [Loadable Function]
`[z, err] = conicalP_1 (...)` [Loadable Function]

These routines compute the conical function $P^1\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhzeta -*- texinfo -*-

`z = hzeta (x, y)` [Loadable Function]
`[z, err] = hzeta (...)` [Loadable Function]

These routines compute the Hurwitz zeta function $\zeta(s, q)$ for $s > 1, q > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`Ai -*- texinfo -*-

`y = airy_Ai (x, mode)` [Loadable Function]
`[y, err] = airy_Ai (...)` [Loadable Function]

These routines compute the Airy function $Ai(x)$ with an accuracy specified by `mode`.

The second argument `mode` must be an integer corresponding to

0 = `GSL`PREC`DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL`PREC`SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi *- texinfo *-

y = airy_Bi (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Bi (...) [Loadable Function]

These routines compute the Airy function Bi(*x*) with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Ai'scaled *- texinfo *-

y = airy_Ai_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Ai_scaled (...) [Loadable Function]

These routines compute a scaled version of the Airy function S'A(*x*) Ai(*x*). For *x*>0 the scaling factor S'A(*x*) is $\exp(+ (2/3) x^{(3/2)})$, and is 1 for *x*<0.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'scaled *- texinfo *-

`y = airy_Bi_scaled (x, mode)` [Loadable Function]

`[y, err] = airy_Bi_scaled (...)` [Loadable Function]

These routines compute a scaled version of the Airy function $S'B(x) Bi(x)$. For $x > 0$ the scaling factor $S'B(x)$ is $\exp(-(2/3) x^{(3/2)})$, and is 1 for $x < 0$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy' Ai' deriv *- texinfo *-

`y = airy_Ai_deriv (x, mode)` [Loadable Function]

`[y, err] = airy_Ai_deriv (...)` [Loadable Function]

These routines compute the Airy function derivative $Ai'(x)$ with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy' Bi' deriv *- texinfo *-

`y = airy_Bi_deriv (x, mode)` [Loadable Function]

`[y, err] = airy_Bi_deriv (...)` [Loadable Function]

These routines compute the Airy function derivative $Bi'(x)$ with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy' Ai' deriv' scaled -*- texinfo -*-

y = airy_Ai_deriv_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Ai_deriv_scaled (...) [Loadable Function]

These routines compute the derivative of the scaled Airy function $S'A(x)$ $Ai(x)$.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy' Bi' deriv' scaled -*- texinfo -*-

y = airy_Bi_deriv_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Bi_deriv_scaled (...) [Loadable Function]

These routines compute the derivative of the scaled Airy function $S'B(x)$ $Bi(x)$.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint' Kcomp -*- texinfo -*-

y = ellint_Kcomp (*x*, *mode*) [Loadable Function]

`[y, err] = ellint_Kcomp (...)` [Loadable Function]

These routines compute the complete elliptic integral $K(k)$

$$K(k) = \int_0^{\pi/2} \frac{dt}{\sqrt{(1 - k^2 \sin^2(t))}}$$

See also:

`ellipj`, `ellipke`

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint'Ecomp *- texinfo *-

`y = ellint_Ecomp (x, mode)` [Loadable Function]

`[y, err] = ellint_Ecomp (...)` [Loadable Function]

These routines compute the complete elliptic integral $E(k)$ to the accuracy specified by the mode variable *mode*.

$$E(k) = \int_0^{\pi/2} \sqrt{(1 - k^2 \sin^2(t))} dt$$

See also:

`ellipj`, `ellipke`

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'zero' Ai *- texinfo *-

y = `airy_zero_Ai` (*n*) [Loadable Function]

[*y*, *err*] = `airy_zero_Ai` (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function $Ai(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'zero' Bi *- texinfo *-

y = `airy_zero_Bi` (*n*) [Loadable Function]

[*y*, *err*] = `airy_zero_Bi` (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function $Bi(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'zero' Ai'deriv *- texinfo *-

y = `airy_zero_Ai_deriv` (*n*) [Loadable Function]

[*y*, *err*] = `airy_zero_Ai_deriv` (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function derivative $Ai(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'zero' Bi'deriv *- texinfo *-

y = `airy_zero_Bi_deriv` (*n*) [Loadable Function]

[*y*, *err*] = `airy_zero_Bi_deriv` (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function derivative $Bi(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel'zero' J0 *- texinfo *-

y = `bessel_zero_J0` (*n*) [Loadable Function]

[*y*, *err*] = `bessel_zero_J0` (...) [Loadable Function]

These routines compute the location of the *s*-th positive zero of the Bessel function $J_0(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`zero`J1 *-*- texinfo -*-*

y = `bessel_zero_J1` (*n*) [Loadable Function]

[*y*, *err*] = `bessel_zero_J1` (...) [Loadable Function]

These routines compute the location of the *s*-th positive zero of the Bessel function $J_1(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi`1`int *-*- texinfo -*-*

y = `psi_1_int` (*n*) [Loadable Function]

[*y*, *err*] = `psi_1_int` (...) [Loadable Function]

These routines compute the Trigamma function $\psi(n)$ for positive integer *n*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta`int *-*- texinfo -*-*

y = `zeta_int` (*n*) [Loadable Function]

[*y*, *err*] = `zeta_int` (...) [Loadable Function]

These routines compute the Riemann zeta function $\zeta(n)$ for integer *n*, $n \in \mathbb{1}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta`int *-*- texinfo -*-*

y = `eta_int` (*n*) [Loadable Function]

[*y*, *err*] = `eta_int` (...) [Loadable Function]

These routines compute the eta function $\eta(n)$ for integer *n*.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre`Plm *-*- texinfo -*-*

y = `legendre_Plm` (*n*, *m*, *x*) [Loadable Function]

[*y*, *err*] = `legendre_Plm` (...) [Loadable Function]

These routines compute the associated Legendre polynomial $P_l^m(x)$ for $m \geq 0$, $l \geq m$, $|x| \leq 1$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre'sphPlm *- texinfo *-

`y = legendre_sphPlm (n, m, x)` [Loadable Function]

`[y, err] = legendre_sphPlm (...)` [Loadable Function]

These routines compute the normalized associated Legendre polynomial $\sqrt{\frac{2l+1}{4\pi}} \sqrt{\frac{(l-m)!}{(l+m)!}} P_l^m(x)$ suitable for use in spherical harmonics. The parameters must satisfy $m \geq 0$, $l \geq m$, $|x| \leq 1$. These routines avoid the overflows that occur for the standard normalization of $P_l^m(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`U *- texinfo *-

`out = hyperg_U (x0, x1, x2)` [Loadable Function]

`[out, err] = hyperg_U (...)` [Loadable Function]

Secondary Confluent Hypergeometric U function A&E 13.1.3 All inputs are double as is the output.

`err` contains an estimate of the absolute error in the value `out.a`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`1F1 *- texinfo *-

`out = hyperg_1F1 (x0, x1, x2)` [Loadable Function]

`[out, err] = hyperg_1F1 (...)` [Loadable Function]

Primary Confluent Hypergeometric U function A&E 13.1.3 All inputs are double as is the output.

`err` contains an estimate of the absolute error in the value `out.a`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgsl'sf *- texinfo *-

`gsl_sf ()` [Loadable Function]

Octave bindings to the GNU Scientific Library. All GSL functions can be called with by the GSL names within octave.

Øclausen *- texinfo *-

`y = clausen (x)` [Loadable Function]

`[y, err] = clausen (...)` [Loadable Function]

The Clausen function is defined by the following integral,

$$Cl_2(x) = - \int_0^x dt \log(2 \sin(t/2))$$

It is related to the dilogarithm by $Cl_2(\theta) = \text{Im Li}_2(\exp(i \theta))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødawson -*- texinfo -*-

`y = dawson (x)` [Loadable Function]

`[y, err] = dawson (...)` [Loadable Function]

The Dawson integral is defined by $\exp(-x^2) \int_0^x \exp(t^2) dt$. A table of Dawson integral can be found in Abramowitz & Stegun, Table 7.5.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'1 -*- texinfo -*-

`y = debye_1 (x)` [Loadable Function]

`[y, err] = debye_1 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'2 -*- texinfo -*-

`y = debye_2 (x)` [Loadable Function]

`[y, err] = debye_2 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'3 -*- texinfo -*-

`y = debye_3 (x)` [Loadable Function]

`[y, err] = debye_3 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ødebye'4 -*- texinfo -*-

`y = debye_4 (x)` [Loadable Function]
`[y, err] = debye_4 (...)` [Loadable Function]

The Debye functions are defined by the integral

$$D_n(x) = n/x^n \int_0^x dt (t^n/(e^t - 1)).$$

For further information see Abramowitz & Stegun, Section 27.1.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf`gsl`-*- texinfo`-*-

`y = erf_gsl (x)` [Loadable Function]
`[y, err] = erf_gsl (...)` [Loadable Function]

These routines compute the error function $\text{erf}(x) = (2/\sqrt{\pi}) \int_0^x dt \exp(-t^2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerfc`gsl`-*- texinfo`-*-

`y = erfc_gsl (x)` [Loadable Function]
`[y, err] = erfc_gsl (...)` [Loadable Function]

These routines compute the complementary error function $\text{erfc}(x) = 1 - \text{erf}(x) = (2/\sqrt{\pi}) \int_x^\infty \exp(-t^2) dt$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog`erfc`-*- texinfo`-*-

`y = log_erfc (x)` [Loadable Function]
`[y, err] = log_erfc (...)` [Loadable Function]

These routines compute the logarithm of the complementary error function $\log(\text{erfc}(x))$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf`Z`-*- texinfo`-*-

`y = erf_Z (x)` [Loadable Function]
`[y, err] = erf_Z (...)` [Loadable Function]

These routines compute the Gaussian probability function $Z(x) = (1/(2\pi)) \exp(-x^2/2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øerf_Q -*- texinfo -*-

`y = erf_Q (x)` [Loadable Function]
`[y, err] = erf_Q (...)` [Loadable Function]

These routines compute the upper tail of the Gaussian probability function $Q(x) = (1/(2\pi)) \int_x^{\infty} dt \exp(-t^2/2)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhazard -*- texinfo -*-

`y = hazard (x)` [Loadable Function]
`[y, err] = hazard (...)` [Loadable Function]

The hazard function for the normal distribution, also known as the inverse Mill's ratio, is defined as $h(x) = Z(x)/Q(x) = \sqrt{2/\pi} \exp(-x^2/2) / \operatorname{erfc}(x/\sqrt{2})$. It decreases rapidly as `x` approaches $-\infty$ and asymptotes to $h(x) \sim x$ as `x` approaches $+\infty$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpm1 -*- texinfo -*-

`y = expm1 (x)` [Loadable Function]
`[y, err] = expm1 (...)` [Loadable Function]

These routines compute the quantity $\exp(x)-1$ using an algorithm that is accurate for small `x`.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel -*- texinfo -*-

`y = exprel (x)` [Loadable Function]
`[y, err] = exprel (...)` [Loadable Function]

These routines compute the quantity $(\exp(x)-1)/x$ using an algorithm that is accurate for small `x`. For small `x` the algorithm is based on the expansion $(\exp(x)-1)/x = 1 + x/2 + x^2/(2*3) + x^3/(2*3*4) + \dots$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel'2 -*- texinfo -*-

`y = exprel_2 (x)` [Loadable Function]

`[y, err] = exprel_2 (...)` [Loadable Function]

These routines compute the quantity $2(\exp(x)-1-x)/x^2$ using an algorithm that is accurate for small x . For small x the algorithm is based on the expansion $2(\exp(x)-1-x)/x^2 = 1 + x/3 + x^2/(3*4) + x^3/(3*4*5) + \dots$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`E1 -*- texinfo -*-

`y = expint_E1 (x)` [Loadable Function]

`[y, err] = expint_E1 (...)` [Loadable Function]

These routines compute the exponential integral $E_1(x)$,

$E_1(x) := \operatorname{Re} \int_1^\infty dt \exp(-xt)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`E2 -*- texinfo -*-

`y = expint_E2 (x)` [Loadable Function]

`[y, err] = expint_E2 (...)` [Loadable Function]

These routines compute the second-order exponential integral $E_2(x)$,

$E_2(x) := \operatorname{Re} \int_1^\infty dt \exp(-xt)/t^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint`Ei -*- texinfo -*-

`y = expint_Ei (x)` [Loadable Function]

`[y, err] = expint_Ei (...)` [Loadable Function]

These routines compute the exponential integral $E_i(x)$,

$E_i(x) := -\operatorname{PV}(\int_{-x}^\infty dt \exp(-t)/t)$

where PV denotes the principal value of the integral.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØShi -*- texinfo -*-

`y = Shi (x)` [Loadable Function]

`[y, err] = Shi (...)` [Loadable Function]

These routines compute the integral $\operatorname{Shi}(x) = \int_0^x dt \sinh(t)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØChi -*- texinfo -*-

`y = Chi (x)` [Loadable Function]
`[y, err] = Chi (...)` [Loadable Function]

These routines compute the integral

$\text{Chi}(x) := \text{Re}[\gamma'E + \log(x) + \int_0^x dt (\cosh[t]-1)/t]$,

where $\gamma'E$ is the Euler constant.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexpint'3 -*- texinfo -*-

`y = expint_3 (x)` [Loadable Function]
`[y, err] = expint_3 (...)` [Loadable Function]

These routines compute the exponential integral $Ei_3(x) = \int_0^x dt \exp(-t^3)$ for $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØSi -*- texinfo -*-

`y = Si (x)` [Loadable Function]
`[y, err] = Si (...)` [Loadable Function]

These routines compute the Sine integral $Si(x) = \int_0^x dt \sin(t)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØCi -*- texinfo -*-

`y = Ci (x)` [Loadable Function]
`[y, err] = Ci (...)` [Loadable Function]

These routines compute the Cosine integral $Ci(x) = -\int_x^\infty dt \cos(t)/t$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øatanint -*- texinfo -*-

`y = atanint (x)` [Loadable Function]
`[y, err] = atanint (...)` [Loadable Function]

These routines compute the Arctangent integral $\text{AtanInt}(x) = \int_0^x dt \arctan(t)/t$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`mhalf -*- texinfo -*-

`y = fermi_dirac_mhalf (x)` [Loadable Function]

`[y, err] = fermi_dirac_mhalf (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{-1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`half -*- texinfo -*-

`y = fermi_dirac_half (x)` [Loadable Function]

`[y, err] = fermi_dirac_half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{1/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi`dirac`3half -*- texinfo -*-

`y = fermi_dirac_3half (x)` [Loadable Function]

`[y, err] = fermi_dirac_3half (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral $F^{3/2}(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`gsl -*- texinfo -*-

`y = gamma_gsl (x)` [Loadable Function]

`[y, err] = gamma_gsl (...)` [Loadable Function]

These routines compute the Gamma function $\Gamma(x)$, subject to `x` not being a negative integer. The function is computed using the real Lanczos method. The maximum value of `x` such that $\Gamma(x)$ is not considered an overflow is given by the macro `GSL_SF_GAMMA_XMAX` and is 171.0.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølngamma`gsl -*- texinfo -*-

`y = lngamma_gsl (x)` [Loadable Function]

`[y, err] = lngamma_gsl (...)` [Loadable Function]

These routines compute the logarithm of the Gamma function, $\log(\Gamma(x))$, subject to `x` not a being negative integer. For `x < 0` the real part of $\log(\Gamma(x))$ is returned, which is equivalent to $\log(|\Gamma(x)|)$. The function is computed using the real Lanczos method.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgammastar *- texinfo *-

`y = gammastar (x)` [Loadable Function]
`[y, err] = gammastar (...)` [Loadable Function]

These routines compute the regulated Gamma Function $\Gamma^*(x)$ for $x > 0$. The regulated gamma function is given by,

$$\Gamma^*(x) = \Gamma(x) / (\sqrt{2\pi} x^{\{x-1/2\}} \exp(-x)) = (1 + (1/12x) + \dots)$$
for x to infity

and is a useful suggestion of Temme.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgammainv'gsl *- texinfo *-

`y = gammainv_gsl (x)` [Loadable Function]
`[y, err] = gammainv_gsl (...)` [Loadable Function]

These routines compute the reciprocal of the gamma function, $1/\Gamma(x)$ using the real Lanczos method.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølambert'W0 *- texinfo *-

`y = lambert_W0 (x)` [Loadable Function]
`[y, err] = lambert_W0 (...)` [Loadable Function]

These compute the principal branch of the Lambert W function, $W^0(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x) \exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W^0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W^{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølambert'Wm1 *- texinfo *-

`y = lambert_Wm1 (x)` [Loadable Function]
`[y, err] = lambert_Wm1 (...)` [Loadable Function]

These compute the secondary real-valued branch of the Lambert W function, $W^{-1}(x)$.

Lambert's W functions, $W(x)$, are defined to be solutions of the equation $W(x) \exp(W(x)) = x$. This function has multiple branches for $x < 0$; however, it has only two real-valued branches. We define $W^0(x)$ to be the principal branch, where $W > -1$ for $x < 0$, and $W^{-1}(x)$ to be the other real branch, where $W < -1$ for $x < 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog_1plusx -*- texinfo -*-

`y = log_1plusx (x)` [Loadable Function]

`[y, err] = log_1plusx (...)` [Loadable Function]

These routines compute $\log(1 + x)$ for $x > -1$ using an algorithm that is accurate for small x .

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølog_1plusx_mx -*- texinfo -*-

`y = log_1plusx_mx (x)` [Loadable Function]

`[y, err] = log_1plusx_mx (...)` [Loadable Function]

These routines compute $\log(1 + x) - x$ for $x > -1$ using an algorithm that is accurate for small x .

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi -*- texinfo -*-

`y = psi (x)` [Loadable Function]

`[y, err] = psi (...)` [Loadable Function]

These routines compute the digamma function $\psi(x)$ for general x , $x \neq 0$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi_1piy -*- texinfo -*-

`y = psi_1piy (x)` [Loadable Function]

`[y, err] = psi_1piy (...)` [Loadable Function]

These routines compute the real part of the digamma function on the line $1 + iy$, $\text{Re}[\psi(1 + iy)]$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron_1 -*- texinfo -*-

`y = synchrotron_1 (x)` [Loadable Function]

`[y, err] = synchrotron_1 (...)` [Loadable Function]

These routines compute the first synchrotron function $x \int_0^x dt K_{5/3}(t)$ for $x \geq 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsynchrotron`2`-*- texinfo -*-

y = `synchrotron_2` (*x*) [Loadable Function]

[*y*, *err*] = `synchrotron_2` (...) [Loadable Function]

These routines compute the second synchrotron function $x K_{2/3}(x)$ for $x \geq 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`2`-*- texinfo -*-

y = `transport_2` (*x*) [Loadable Function]

[*y*, *err*] = `transport_2` (...) [Loadable Function]

These routines compute the transport function $J(2,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`3`-*- texinfo -*-

y = `transport_3` (*x*) [Loadable Function]

[*y*, *err*] = `transport_3` (...) [Loadable Function]

These routines compute the transport function $J(3,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`4`-*- texinfo -*-

y = `transport_4` (*x*) [Loadable Function]

[*y*, *err*] = `transport_4` (...) [Loadable Function]

These routines compute the transport function $J(4,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtransport`5`-*- texinfo -*-

`y = transport_5 (x)` [Loadable Function]
`[y, err] = transport_5 (...)` [Loadable Function]

These routines compute the transport function $J(5,x)$.

The transport functions $J(n,x)$ are defined by the integral representations $J(n,x) := \int_0^x dt t^n e^t / (e^t - 1)^2$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øsinc'gsl -*- texinfo -*-

`y = sinc_gsl (x)` [Loadable Function]
`[y, err] = sinc_gsl (...)` [Loadable Function]

These routines compute $\text{sinc}(x) = \sin(\pi x) / (\pi x)$ for any value of `x`.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnsinh -*- texinfo -*-

`y = lnsinh (x)` [Loadable Function]
`[y, err] = lnsinh (...)` [Loadable Function]

These routines compute $\log(\sinh(x))$ for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølncosh -*- texinfo -*-

`y = lncosh (x)` [Loadable Function]
`[y, err] = lncosh (...)` [Loadable Function]

These routines compute $\log(\cosh(x))$ for any `x`.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta -*- texinfo -*-

`y = zeta (x)` [Loadable Function]
`[y, err] = zeta (...)` [Loadable Function]

These routines compute the Riemann zeta function $\zeta(s)$ for arbitrary `s`, $s \in \mathbb{R}$.

The Riemann zeta function is defined by the infinite sum $\zeta(s) = \sum_{k=1}^{\infty} k^{-s}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta *-*- texinfo -**

`y = eta (x)` [Loadable Function]
`[y, err] = eta (...)` [Loadable Function]

These routines compute the eta function $\eta(s)$ for arbitrary s .

The eta function is defined by $\eta(s) = (1-2^{1-s}) \zeta(s)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Jn *-*- texinfo -**

`y = bessel_Jn (n, x)` [Loadable Function]
`[y, err] = bessel_Jn (...)` [Loadable Function]

These routines compute the regular cylindrical Bessel function of order n , $J_n(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Yn *-*- texinfo -**

`y = bessel_Yn (n, x)` [Loadable Function]
`[y, err] = bessel_Yn (...)` [Loadable Function]

These routines compute the irregular cylindrical Bessel function of order n , $Y_n(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`In *-*- texinfo -**

`y = bessel_In (n, x)` [Loadable Function]
`[y, err] = bessel_In (...)` [Loadable Function]

These routines compute the regular modified cylindrical Bessel function of order n , $I_n(x)$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`In`scaled *-*- texinfo -**

`y = bessel_In_scaled (n, x)` [Loadable Function]
`[y, err] = bessel_In_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified cylindrical Bessel function of order n , $\exp(-|x|) I_n(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Kn -*- texinfo -*-

`y = bessell_Kn (n, x)` [Loadable Function]
`[y, err] = bessell_Kn (...)` [Loadable Function]

These routines compute the irregular modified cylindrical Bessel function of order n , $K_n(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Kn`scaled -*- texinfo -*-

`y = bessell_Kn_scaled (n, x)` [Loadable Function]
`[y, err] = bessell_Kn_scaled (...)` [Loadable Function]

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`jl -*- texinfo -*-

`y = bessell_jl (n, x)` [Loadable Function]
`[y, err] = bessell_jl (...)` [Loadable Function]

These routines compute the regular spherical Bessel function of order l , $j_l(x)$, for $l \geq 0$ and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`yl -*- texinfo -*-

`y = bessell_yl (n, x)` [Loadable Function]
`[y, err] = bessell_yl (...)` [Loadable Function]

These routines compute the irregular spherical Bessel function of order l , $y_l(x)$, for $l \geq 0$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`il`scaled -*- texinfo -*-

`y = bessell_il_scaled (n, x)` [Loadable Function]
`[y, err] = bessell_il_scaled (...)` [Loadable Function]

These routines compute the scaled regular modified spherical Bessel function of order l , $\exp(-|x|) i_l(x)$

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel'kl'scaled *- texinfo *-

`y = bessell_scaled (n, x)` [Loadable Function]
`[y, err] = bessell_scaled (...)` [Loadable Function]

These routines compute the scaled irregular modified spherical Bessel function of order l , $\exp(x) k_l(x)$, for $x > 0$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexprel'n *- texinfo *-

`y = exprel_n (n, x)` [Loadable Function]
`[y, err] = exprel_n (...)` [Loadable Function]

These routines compute the N -relative exponential, which is the n -th generalization of the functions `gsl_sf_exprel` and `gsl_sf_exprel2`. The N -relative exponential is given by,

$$\text{exprel}'N(x) = N! / x^N (\exp(x) - \sum_{k=0}^{N-1} x^k / k!) = 1 + x / (N+1) + x^2 / ((N+1)(N+2)) + \dots = {}_1F_1(1, 1+N, x)$$

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi'dirac'int *- texinfo *-

`y = fermi_dirac_int (n, x)` [Loadable Function]
`[y, err] = fermi_dirac_int (...)` [Loadable Function]

These routines compute the complete Fermi-Dirac integral with an integer index of j , $F_j(x) = (1/\Gamma(j+1)) \int_0^\infty dt (t^j / (\exp(t-x)+1))$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øtaylorcoeff *- texinfo *-

`y = taylorcoeff (n, x)` [Loadable Function]
`[y, err] = taylorcoeff (...)` [Loadable Function]

These routines compute the Taylor coefficient $x^n / n!$ for $x \geq 0$, $n \geq 0$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre'Pl *- texinfo *-

`y = legendre_Pl (n, x)` [Loadable Function]
`[y, err] = legendre_Pl (...)` [Loadable Function]

These functions evaluate the Legendre polynomial $P_l(x)$ for a specific value of l , x subject to $l \geq 0$, $|x| \leq 1$

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre_Ql *- texinfo *-

y = `legendre_Ql` (*n*, *x*) [Loadable Function]

[*y*, *err*] = `legendre_Ql` (...) [Loadable Function]

These routines compute the Legendre function $Q_l(x)$ for $x > -1$, $x \neq 1$ and $l \geq 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi_n *- texinfo *-

y = `psi_n` (*n*, *x*) [Loadable Function]

[*y*, *err*] = `psi_n` (...) [Loadable Function]

These routines compute the polygamma function $\psi^{(m)}(x)$ for $m \geq 0$, $x > 0$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Jnu *- texinfo *-

z = `bessel_Jnu` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Jnu` (...) [Loadable Function]

These routines compute the regular cylindrical Bessel function of fractional order *nu*, $J_\nu(x)$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Ynu *- texinfo *-

z = `bessel_Ynu` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Ynu` (...) [Loadable Function]

These routines compute the irregular cylindrical Bessel function of fractional order *nu*, $Y_\nu(x)$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel_Inu *- texinfo *-

z = `bessel_Inu` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Inu` (...) [Loadable Function]

These routines compute the regular modified Bessel function of fractional order *nu*, $I_\nu(x)$ for $x > 0$, $u > 0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Inu`scaled -*- texinfo -*-

z = `bessel_Inu_scaled` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Inu_scaled` (...) [Loadable Function]

These routines compute the scaled regular modified Bessel function of fractional order *nu*, $\exp(-|x|)I_\nu(x)$ for $x>0$, $u>0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Knu -*- texinfo -*-

z = `bessel_Knu` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Knu` (...) [Loadable Function]

These routines compute the irregular modified Bessel function of fractional order *nu*, $K_\nu(x)$ for $x>0$, $u>0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`lnKnu -*- texinfo -*-

z = `bessel_lnKnu` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_lnKnu` (...) [Loadable Function]

These routines compute the logarithm of the irregular modified Bessel function of fractional order *nu*, $\ln(K_\nu(x))$ for $x>0$, $u>0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel`Knu`scaled -*- texinfo -*-

z = `bessel_Knu_scaled` (*x*, *y*) [Loadable Function]

[*z*, *err*] = `bessel_Knu_scaled` (...) [Loadable Function]

These routines compute the scaled irregular modified Bessel function of fractional order *nu*, $\exp(+|x|)K_\nu(x)$ for $x>0$, $u>0$.

err contains an estimate of the absolute error in the value *z*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øexp`mult -*- texinfo -*-

`z = exp_mult (x, y)` [Loadable Function]

`[z, err] = exp_mult (...)` [Loadable Function]

These routines exponentiate x and multiply by the factor y to return the product $y \exp(x)$.

`err` contains an estimate of the absolute error in the value z .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øfermi'dirac'inc'0 *- texinfo *-

`z = fermi_dirac_inc_0 (x, y)` [Loadable Function]

`[z, err] = fermi_dirac_inc_0 (...)` [Loadable Function]

These routines compute the incomplete Fermi-Dirac integral with an index of zero, $F_0(x, b) = \ln(1 + e^{\{b-x\}}) - (b-x)$.

`err` contains an estimate of the absolute error in the value z .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpoch *- texinfo *-

`z = poch (x, y)` [Loadable Function]

`[z, err] = poch (...)` [Loadable Function]

These routines compute the Pochhammer symbol

$(a)_x := \Gamma(a + x)/\Gamma(a)$,

subject to a and $a+x$ not being negative integers. The Pochhammer symbol is also known as the Apell symbol.

`err` contains an estimate of the absolute error in the value z .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnpoch *- texinfo *-

`z = ln_poch (x, y)` [Loadable Function]

`[z, err] = ln_poch (...)` [Loadable Function]

These routines compute the logarithm of the Pochhammer symbol, $\log((a)_x) = \log(\Gamma(a + x)/\Gamma(a))$ for $a > 0$, $a+x > 0$.

`err` contains an estimate of the absolute error in the value z .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpochrel *- texinfo *-

`z = pochrel (x, y)` [Loadable Function]

`[z, err] = pochrel (...)` [Loadable Function]

These routines compute the relative Pochhammer symbol $((a, x) - 1)/x$ where $(a, x) = (a)_x := \Gamma(a + x)/\Gamma(a)$.

`err` contains an estimate of the absolute error in the value z .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`Q *- texinfo *-

`z = gamma_inc_Q (x, y)` [Loadable Function]
`[z, err] = gamma_inc_Q (...)` [Loadable Function]

These routines compute the normalized incomplete Gamma Function $Q(a,x) = 1/\Gamma(a) \int_0^x dt t^{a-1} \exp(-t)$ for $a > 0, x \geq 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc`P *- texinfo *-

`z = gamma_inc_P (x, y)` [Loadable Function]
`[z, err] = gamma_inc_P (...)` [Loadable Function]

These routines compute the complementary normalized incomplete Gamma Function $P(a,x) = 1/\Gamma(a) \int_x^\infty dt t^{a-1} \exp(-t)$ for $a > 0, x \geq 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øgamma`inc *- texinfo *-

`z = gamma_inc (x, y)` [Loadable Function]
`[z, err] = gamma_inc (...)` [Loadable Function]

These functions compute the incomplete Gamma Function the normalization factor included in the previously defined functions: $\Gamma(a,x) = \int_0^x dt t^{a-1} \exp(-t)$ for a real and $x \geq 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbeta`gsl *- texinfo *-

`z = beta_gsl (x, y)` [Loadable Function]
`[z, err] = beta_gsl (...)` [Loadable Function]

These routines compute the Beta Function, $B(a,b) = \Gamma(a)\Gamma(b)/\Gamma(a+b)$ for $a > 0, b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølnbeta *- texinfo *-

`z = lnbeta (x, y)` [Loadable Function]
`[z, err] = lnbeta (...)` [Loadable Function]

These routines compute the logarithm of the Beta Function, $\log(B(a,b))$ for $a > 0, b > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg'0F1 -*- texinfo -*-

`z = hyperg_0F1 (x, y)` [Loadable Function]
`[z, err] = hyperg_0F1 (...)` [Loadable Function]

These routines compute the hypergeometric function ${}_0F_1(c,x)$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP'half -*- texinfo -*-

`z = conicalP_half (x, y)` [Loadable Function]
`[z, err] = conicalP_half (...)` [Loadable Function]

These routines compute the irregular Spherical Conical Function $P^{-1/2}\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP'mhalf -*- texinfo -*-

`z = conicalP_mhalf (x, y)` [Loadable Function]
`[z, err] = conicalP_mhalf (...)` [Loadable Function]

These routines compute the regular Spherical Conical Function $P^{-1/2}\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP'0 -*- texinfo -*-

`z = conicalP_0 (x, y)` [Loadable Function]
`[z, err] = conicalP_0 (...)` [Loadable Function]

These routines compute the conical function $P^0\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

ØconicalP'1 -*- texinfo -*-

`z = conicalP_1 (x, y)` [Loadable Function]
`[z, err] = conicalP_1 (...)` [Loadable Function]

These routines compute the conical function $P^1\{-1/2 + i\lambda\}(x)$ for $x > -1$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhzeta -*- texinfo -*-

`z = hzeta (x, y)` [Loadable Function]
`[z, err] = hzeta (...)` [Loadable Function]

These routines compute the Hurwitz zeta function $\zeta(s, q)$ for $s > 1, q > 0$.

`err` contains an estimate of the absolute error in the value `z`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`Ai`-*` texinfo`-*`

`y = airy_Ai (x, mode)` [Loadable Function]
`[y, err] = airy_Ai (...)` [Loadable Function]

These routines compute the Airy function $\text{Ai}(x)$ with an accuracy specified by `mode`.

The second argument `mode` must be an integer corresponding to

0 = `GSL`PREC`DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL`PREC`SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL`PREC`APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`Bi`-*` texinfo`-*`

`y = airy_Bi (x, mode)` [Loadable Function]
`[y, err] = airy_Bi (...)` [Loadable Function]

These routines compute the Airy function $\text{Bi}(x)$ with an accuracy specified by `mode`.

The second argument `mode` must be an integer corresponding to

0 = `GSL`PREC`DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL`PREC`SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL`PREC`APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

`err` contains an estimate of the absolute error in the value `y`.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`Ai`scaled`-*` texinfo`-*`

`y = airy_Ai_scaled (x, mode)` [Loadable Function]
`[y, err] = airy_Ai_scaled (...)` [Loadable Function]

These routines compute a scaled version of the Airy function $S'A(x)$ $Ai(x)$. For $x > 0$ the scaling factor $S'A(x)$ is $\exp(+ (2/3) x^{(3/2)})$, and is 1 for $x < 0$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'scaled *- texinfo *-

`y = airy_Bi_scaled (x, mode)` [Loadable Function]
`[y, err] = airy_Bi_scaled (...)` [Loadable Function]

These routines compute a scaled version of the Airy function $S'B(x)$ $Bi(x)$. For $x > 0$ the scaling factor $S'B(x)$ is $\exp(- (2/3) x^{(3/2)})$, and is 1 for $x < 0$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy' Ai'deriv *- texinfo *-

`y = airy_Ai_deriv (x, mode)` [Loadable Function]
`[y, err] = airy_Ai_deriv (...)` [Loadable Function]

These routines compute the Airy function derivative $Ai'(x)$ with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'deriv *- texinfo *-

y = airy_Bi_deriv (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Bi_deriv (...) [Loadable Function]

These routines compute the Airy function derivative Bi'(x) with an accuracy specified by *mode*.

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Ai'deriv'scaled *- texinfo *-

y = airy_Ai_deriv_scaled (*x*, *mode*) [Loadable Function]

[*y*, *err*] = airy_Ai_deriv_scaled (...) [Loadable Function]

These routines compute the derivative of the scaled Airy function S'A(x) Ai(x).

The second argument *mode* must be an integer corresponding to

0 = GSL'PREC'DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL'PREC'SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL'PREC'APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'Bi'deriv'scaled *- texinfo *-

`y = airy_Bi_deriv_scaled (x, mode)` [Loadable Function]
`[y, err] = airy_Bi_deriv_scaled (...)` [Loadable Function]

These routines compute the derivative of the scaled Airy function $S'B(x)$ $Bi(x)$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint'Kcomp -*- texinfo -*-

`y = ellint_Kcomp (x, mode)` [Loadable Function]
`[y, err] = ellint_Kcomp (...)` [Loadable Function]

These routines compute the complete elliptic integral $K(k)$

$$K(k) = \int_0^{\pi/2} \frac{dt}{\sqrt{(1 - k^2 \sin^2(t))}}$$

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = `GSL'PREC'DOUBLE`

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = `GSL'PREC'SINGLE`

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = `GSL'PREC'APPROX`

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øellint'Ecomp -*- texinfo -*-

`y = ellint_Ecomp (x, mode)` [Loadable Function]
`[y, err] = ellint_Ecomp (...)` [Loadable Function]

These routines compute the complete elliptic integral $E(k)$ to the accuracy specified by the mode variable *mode*.

$$E(k) = \int_0^{\pi/2} \sqrt{(1 - k^2 \sin^2(t))} dt$$

The notation used here is based on Carlson, *Numerische Mathematik* 33 (1979) and differs slightly from that used by Abramowitz & Stegun, where the functions are given in terms of the parameter $m = k^2$.

The second argument *mode* must be an integer corresponding to

0 = GSL`PREC`DOUBLE

Double-precision, a relative accuracy of approximately $2 * 10^{-16}$.

1 = GSL`PREC`SINGLE

Single-precision, a relative accuracy of approximately 10^{-7} .

2 = GSL`PREC`APPROX

Approximate values, a relative accuracy of approximately $5 * 10^{-4}$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Ai -*- texinfo -*-

y = airy_zero_Ai (*n*) [Loadable Function]
 [*y*, *err*] = airy_zero_Ai (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function Ai(*x*).

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Bi -*- texinfo -*-

y = airy_zero_Bi (*n*) [Loadable Function]
 [*y*, *err*] = airy_zero_Bi (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function Bi(*x*).

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy`zero`Ai`deriv -*- texinfo -*-

y = airy_zero_Ai_deriv (*n*) [Loadable Function]
 [*y*, *err*] = airy_zero_Ai_deriv (...) [Loadable Function]

These routines compute the location of the *s*-th zero of the Airy function derivative Ai(*x*).

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øairy'zero'Bi'deriv *- texinfo *-

`y = airy_zero_Bi_deriv (n)` [Loadable Function]
`[y, err] = airy_zero_Bi_deriv (...)` [Loadable Function]

These routines compute the location of the s -th zero of the Airy function derivative $\text{Bi}(x)$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel'zero'J0 *- texinfo *-

`y = bessel_zero_J0 (n)` [Loadable Function]
`[y, err] = bessel_zero_J0 (...)` [Loadable Function]

These routines compute the location of the s -th positive zero of the Bessel function $J_0(x)$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øbessel'zero'J1 *- texinfo *-

`y = bessel_zero_J1 (n)` [Loadable Function]
`[y, err] = bessel_zero_J1 (...)` [Loadable Function]

These routines compute the location of the s -th positive zero of the Bessel function $J_1(x)$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øpsi'1'int *- texinfo *-

`y = psi_1_int (n)` [Loadable Function]
`[y, err] = psi_1_int (...)` [Loadable Function]

These routines compute the Trigamma function $\psi_1(n)$ for positive integer n .

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øzeta'int *- texinfo *-

`y = zeta_int (n)` [Loadable Function]
`[y, err] = zeta_int (...)` [Loadable Function]

These routines compute the Riemann zeta function $\zeta(n)$ for integer n , $n \geq 1$.

`err` contains an estimate of the absolute error in the value y .

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øeta`int`-*`- texinfo`-*`-

`y = eta_int (n)` [Loadable Function]
`[y, err] = eta_int (...)` [Loadable Function]

These routines compute the eta function $\eta(n)$ for integer n .
err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre`Plm`-*`- texinfo`-*`-

`y = legendre_Plm (n, m, x)` [Loadable Function]
`[y, err] = legendre_Plm (...)` [Loadable Function]

These routines compute the associated Legendre polynomial $P_l^m(x)$ for $m \geq 0$, $l \geq m$, $|x| \leq 1$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Ølegendre`sphPlm`-*`- texinfo`-*`-

`y = legendre_sphPlm (n, m, x)` [Loadable Function]
`[y, err] = legendre_sphPlm (...)` [Loadable Function]

These routines compute the normalized associated Legendre polynomial $\sqrt{\frac{2l+1}{4\pi}} \sqrt{\frac{(l-m)!}{(l+m)!}} P_l^m(x)$ suitable for use in spherical harmonics. The parameters must satisfy $m \geq 0$, $l \geq m$, $|x| \leq 1$. These routines avoid the overflows that occur for the standard normalization of $P_l^m(x)$.

err contains an estimate of the absolute error in the value *y*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`U`-*`- texinfo`-*`-

`out = hyperg_U (x0, x1, x2)` [Loadable Function]
`[out, err] = hyperg_U (...)` [Loadable Function]

Secondary Confluent Hypergeometric U function A&E 13.1.3 All input are double as is the output.

err contains an estimate of the absolute error in the value *out.a*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.

Øhyperg`1F1`-*`- texinfo`-*`-

`out = hyperg_1F1 (x0, x1, x2)` [Loadable Function]
`[out, err] = hyperg_1F1 (...)` [Loadable Function]

Primary Confluent Hypergeometric U function A&E 13.1.3 All inputs are double as is the output.

err contains an estimate of the absolute error in the value *out.a*.

This function is from the GNU Scientific Library, see <http://www.gnu.org/software/gsl/> for documentation.